Mark schemes

## Q1.

## Alternative method 1

$$
\begin{gathered}
180 \div(5+7) \text { or } 180 \div 12 \text { or } 15 \\
\text { oe }
\end{gathered}
$$

## $5 \times$ their 15 <br> or $180-7 \times$ their 15 or 75

oe

180 - their $75-20$
or 180 - 95
oe

85

Alternative method 2
$x+\frac{7 x}{5}=180$
or $\frac{5 y}{7}+y=180$ or $y=105$
oe correct elimination of a variable from equations $x+y=$ 180 and $7 x=5 y$

$$
\begin{gathered}
(x=) 180 \times \frac{5}{12} \text { or }(x=) 75 \\
o e
\end{gathered}
$$

180 - their $75-20$
or 180 - 95
oe

85

Q2.
$X Y Z=110$ stated or shown or $B X Z=30$ stated or shown
$A B X$ and $X Z B=80$
$X Y Z=110$ stated or shown and $B X Z=30$ stated or shown
$40^{\circ}$
Must be from correct work
Answer only B1

B1

## Alternative Method

$B Z Y=110$ stated or shown or $B X Z=30$ stated or shown
$B X Y=70$ stated or shown and $B X Z=30$ stated or shown
$40^{\circ}$
Must be from correct work
Answer only B1

Q3.
angle $A B C=x$
angle $B A C=x$ and
alternate segment theorem
angle $A B C=x$ and
angle $B A C=x$ and
alternate segment theorem and two equal angles so isosceles ( $A C=B C$ )

Q4.
(a) 35
(b) 100

Angle at centre twice angle on circumference
Must use words 'centre' and 'circumference' (or 'perimeter')
Allow poor spelling even though both words given oe (strand) (i)

B1

B1
$2 x+y+20=180$
or
$x+2 y+y+40=180$
or
$2 x+y+20=x+2 y+y+40$
or
$2 x+y+20+x+2 y+y+40=360$
oe
Another of these equations
$2 x+y+20=180$
or
$x+2 y+y+40=180$
or
$2 x+y+20=x+2 y+y+40$
or
$2 x+y+20+x+2 y+y+40=360$
oe
these simplify to ...
$2 x+y=160$ or
$x+3 y=140$ or
$x-2 y=20$ or
$3 x+4 y=300$
equating coefficients and elimination of $x$ or $y$ for their equations
e.g.
$x+3 y=140$ and $6 x+3 y=480$
or
$2 x+6 y=280$ and $2 x+y=160$
rearrangement and substitution for their equations
e.g.
$y=160-2 x$ and $x+3(160-2 x)=140$
or
$x=140-3 y$ and $2(140-3 y)+y=160$
Allow one numerical error for the 3rd M1, but not an error in method (e.g. adding equations when they ought to be subtracted is an error in method, so MO)

```
\(5 x=340\) or \(5 y=120\)
ft their elimination or substitution
```

$x=68$ and $y=24$

Q6.

Alternate segment (theorem)
B1dep

## Additional Guidance

65 alternative segment (theorem)

65 alternate angles

Q7.
Angle $C A D=46$ or
Angle $A C D=37$ or
Angle CDE $=83$ or $(37+46)$ or
Angle $A D C=97$ or 180-(37+46)
Any of these angles correctly marked or named ... could be on diagram

$$
\text { Angle } D C E=46 \text { or }
$$

Angle $A C E=83$ or $(37+46)$

51

Q8.
Alternative method 1

$$
x+y+70=180
$$

or $x+2 y+40=180$
oe

```
\(x+y=110\)
and \(x+2 y=140\)
\(2 x+2 y=220\)
and \(x+2 y=140\)
oe
Collects terms and equates coefficients
Equations may be implied from 110 or 140 on diagram in correct place
```

$$
x=80 \text { or } y=30
$$

$x=80$ and $y=30$

## Alternative method 2

$$
\begin{aligned}
& x+y+70=180 \\
& \text { or } x+y+70+x+2 y+40=360
\end{aligned}
$$

oe

```
\(2 x+2 y=220\)
and \(2 x+3 y=250\)
\(3 x+3 y=330\)
and \(2 x+3 y=250\)
                    oe
                    Collects terms and equates coefficients
                    Equations may be implied from 110 or 140 on diagram in
                    correct place
```

$x=80$ or $y=30$
$x=80$ and $y=30$

## Alternative method 3

$x+2 y+40=180$
or $x+y+70+x+2 y+40=360$
oe
$2 x+4 y=280$
and $2 x+3 y=250$
$3 x+6 y=420$
and $4 x+6 y=500$
oe
Collects terms and equates coefficients
Equations may be implied from 110 or 140 on diagram in correct place
$x=80$ or $y=30$
$x=80$ and $y=30$

## Alternative method 4

$$
\begin{array}{r}
x+y+70=180 \\
\text { or } x+2 y+40=180 \\
\text { oe }
\end{array}
$$

$$
\begin{aligned}
& 2 y+40-(y+70)=0 \\
& \text { or } 2 x+140-(x+40)=360-180 \\
& \text { oe } \\
& \quad \text { Eliminates a variable }
\end{aligned}
$$

$x=80$ or $y=30$
$x=80$ and $y=30$

## Additional Guidance

$y=30$ must come from correct equations not from $x+2 y=70$ and $x+y=40$

Q9.
Join BD
Angle $B D C=2 x$
Alternate segment theorem

Angle $B D O=x$

Angle $D B O=x$
Isosceles triangle $B O D$

Angle $B O D=180-2 x$
Angle sum of triangle BOD
$y=360-90-90-(180-2 x)$
$y=2 x$
Angle sum of quadrilateral $A B O D$
$y=2 x$ clearly shown from simplification

Must have at least two different reasons stated in the proof

## Alternative method 1

Angle $O B C=90-2 x$
Tangent-radius property

Angle OCB $=90-2 x$
Isosceles $\triangle O B C$

Angle $O C D=x$
Isosceles $\triangle O C D$

```
Angle \(B C D=90-2 x+x\)
\[
=90-x
\]
```

hence

Angle $B O D=180-2 x$
Angle at centre $=2 \times$ angle at circumference
$y=360-90-90-(180-2 x)$
$y=2 x$
Angle sum of quadrilateral $A B O D$
$y=2 x$ clearly shown from simplification

Must have at least two different reasons stated in the proof

## Alternative method 2

Angle $O B C=90-2 x$
Tangent-radius property

Angle $O C B=90-2 x$
Isosceles $\triangle O B C$

Angle $O C D=x$
Isosceles $\triangle O C D$

Angle $B C D=90-2 x+x$

$$
=90-x
$$

hence

Angle $B O D=180-2 x$
Angle at centre $=2 \times$ angle at circumference

Angle $B O D=360-90-90-y$

$$
=180-y
$$

hence $y=2 x$

Angle sum of quadrilateral $A B O D$
$y=2 x$ clearly shown from simplification

Must have at least two different reasons stated in the proof

## Alternative method 3

Angle $O B C=90-2 x$
Tangent-radius property

$$
\text { Angle } O C B=90-2 x
$$

Isosceles $\triangle O B C$

## Angle $O C D=x$

Isosceles $\triangle O C D$

$$
\text { Angle } \begin{aligned}
B C D & =90-2 x+x \\
& =90-x
\end{aligned}
$$

```
\(y=360-90-(90-2 x)-(90-x)-x-90\)
hence \(y=2 x\)
```

Angle sum of quadrilateral $A B C D$
$y=2 x$ clearly shown from simplification

Must have at least two different reasons stated in the proof

## Alternative method 4

Angle $B O D=180-y$
Angle sum of quadrilateral $A B O D$

Angle $O C D=x$
Isosceles $\triangle O C D$

Angle $O B C=90-2 x$
Tangent-radius property

Angle $B C O=90-2 x$
hence
Angle $B O D$ reflex $=360-(90-2 x)-(90-2 x)-x-x=180+2 x$
Isosceles $\triangle O B C$
Angle sum of quadrilateral $B O D C$
... this can also come from Angle BOC (4x) + Angle DOC (180-2x)
$180-y+180+2 x=360$
hence $y=2 x$
Angles round a point
$y=2 x$ clearly shown from rearranging

Must have at least two different reasons stated in the proof

Q10.
(a) 70

May be on diagram
(Opposite angles of) cyclic quadrilateral (add up to $180^{\circ}$ )
Dependent on 70
In a quadrilateral in a circle the opposite angles add up to $180^{\circ}$
(b) One correct angle
$D A E=70$ or $B A D=25$ or $D B C=70$
Angles can ft from their 70 in (a)

Two correct angles
$D A E=70$ or $B A D=25$ or $D B C=70$ or $A D E=40$

Three correct angles
$D A E=70$ or $B A D=25$ or $D B C=70$ or $A D E=40$ or $B D C=$ 95 or $B A E=95$

15

## Q11.

90 seen or implied
90 may be on diagram
or may implied by use of Pythagoras or trigonometry
$8.3^{2}+5.2^{2}$
$\sin 32 .(067 \ldots)$ or $\cos 57 .(9326 \ldots)=\frac{5.2}{O B}$
or $\cos 32 .(067 \ldots)$ or $\sin 57 .(9326 \ldots)=\frac{8.3}{O B}$
$\sqrt{8.3^{2}+5.2^{2}}$

$$
\begin{aligned}
& \frac{5.2}{\sin 32 .(067 . .)} \text { or } \frac{5.2}{\cos 57 .(9326 . .)} \\
& \frac{8.3}{\text { or }^{\cos 32 .(067 . .)}} \text { or } \frac{8.3}{\sin 57 .(9326 \ldots)}
\end{aligned}
$$

$9.79 \ldots$ or 9.8
Accept 10 if working seen

Q12.
$A D$

Q13.
43

Alternate segment (theorem)
Strand (i) Do not accept Alternate
Dependent on B1
Q1

Q14.
(a) 70
(b) $A D E=34$
or $A E D=180-70$ or 110
or $A D C=180-70-34$ or 76
Angles seen on diagram must be in correct place
$A D E=34$
and $A E D=180-70$ or 110

36

Q15.
(a) 56
(b) 70

Alternate segment (theorem)
Strand (i)
Dependent on B1
Q1dep
(c) $2 \times 47$ or 94
or Angle BOA $=47$
or Angle BOC $=47$
or Angle BAC $=47$
or Angle BCA = 47
May be on diagram (obtuse angle)

90 or right angle symbol seen at A or
C
or 180-90-47
or $(180-2 \times 47) \div 2$
oe

43

Q16.
(a) 64

Alternate segment (theorem)
(b) 97

Q17.
Alternative method 1
$B D C=24$
May be on the diagram
$D F C=\frac{180-24}{2}$
or $D C F=\frac{180-24}{2}$
or $\frac{156}{2}$ or 78
May be on the diagram
Finding a base angle in triangle CDF

```
(3x =) 180 - their 78
or (3x =) 24 + their 78
or (3x=) 102
```

oe
May be on the diagram

34
May be on the diagram

## Alternative method 2

$B D C=24$
May be on the diagram
$D F C=180-3 x$
May be on the diagram
$2(180-3 x)+24=180$ or $360-6 x+24=180$
or $3 x+78=180$ or $(3 x=) 102$
oe
M1dep
34
May be on the diagram

## Additional Guidance

If angles in the same segment are not used i.e. all the working is using triangle $A B F$ then award maximum of 2 marks

If triangle $A B F$ is assumed to be isosceles and there is no evidence of angle $B D C=24$ being used then award maximum of 2 marks

If triangle $A B F$ is used as isosceles and correctly justified then all marks are available e.g. 'triangle $A B F$ is similar to triangle CDF'

Answer of 34 does not imply full marks
Answer of 34 with no working
'their 78' must come from an attempt to calculate $\frac{180-24}{2}$
Angles must be clearly identified e.g. $D=24$

24 (unless shown on diagram)

